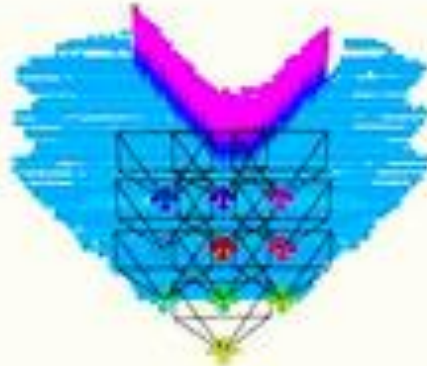


Autonomous Exploration

Tobias Lübke

Seminar: Robot Perception & Intelligence

Munich, 02. December 2024



Motivation

Space Exploration [14]



Search and Rescue Missions [15]



Outline



Challenges in Autonomous Exploration



Key Concepts of Exploration Strategies



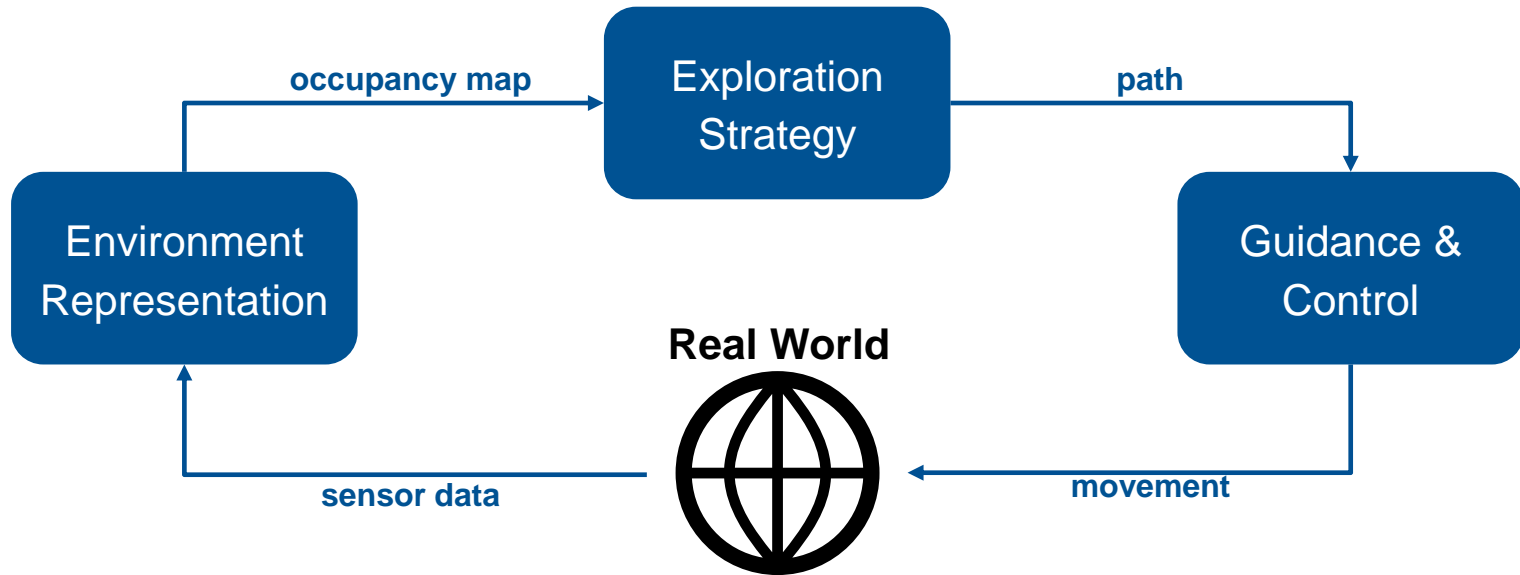
Existing Work & Results

- Receding Horizon Next Best View
- Frontier-based Information-driven Exploration
- FUEL: Fast UAV Exploration

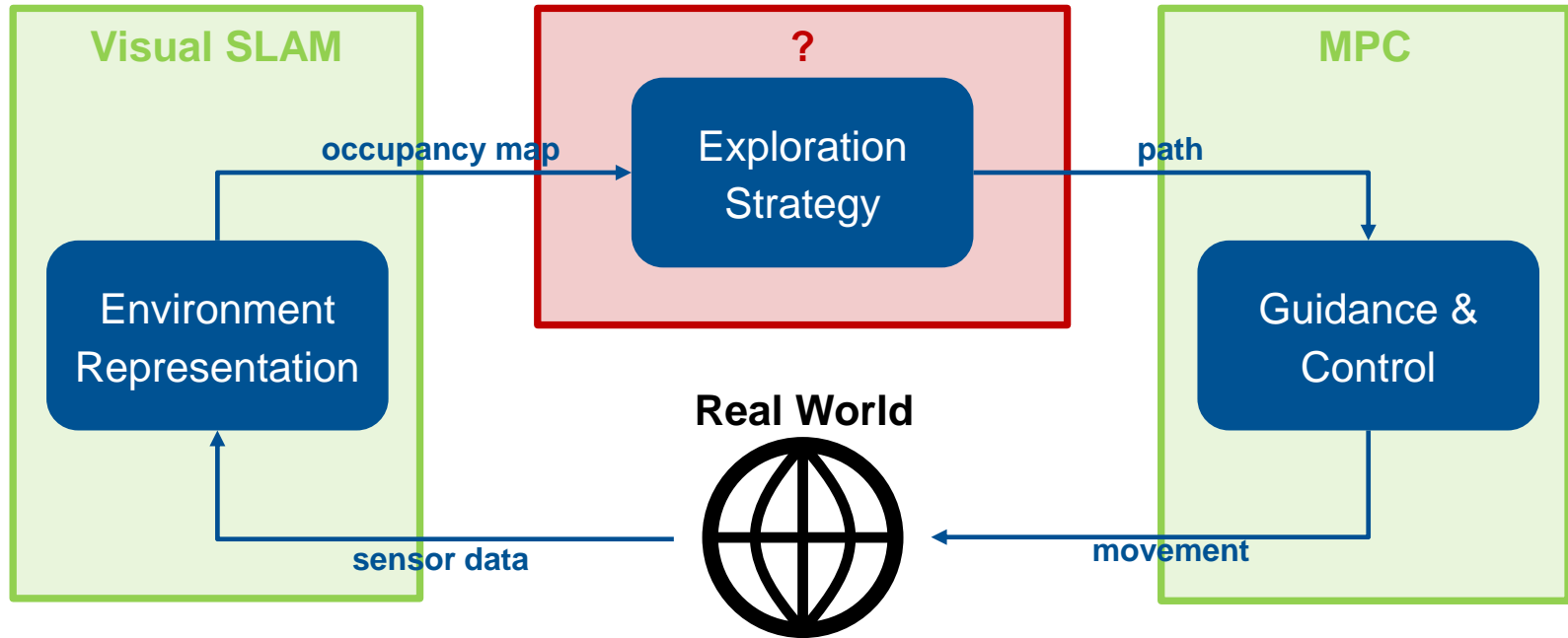


Conclusions & Further Work

Challenges in Autonomous Exploration



Challenges in Autonomous Exploration



Key Concepts of Exploration Strategies



Candidate Generation:

sampling-based / frontier-based



Utility Measure:

volumetric / entropy-based / travel time / etc.



Optimization:

global strategy / greedy strategy

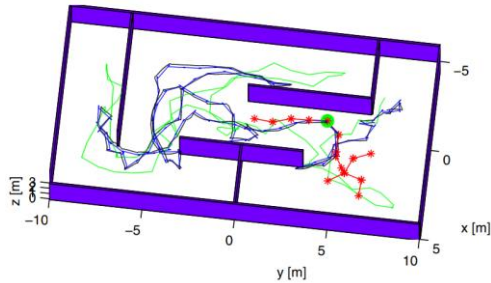


Path Planning:

RRT / RRT* / Dijkstra / A* / etc.

Existing Work

I



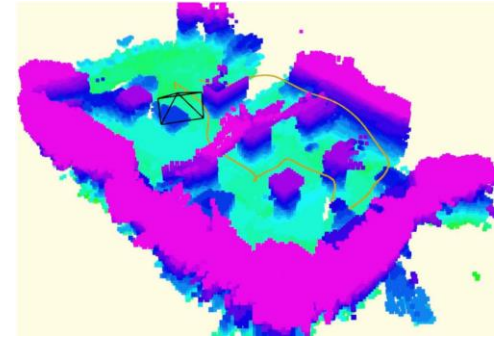
Receding Horizon Next Best View Planner
(2016)

II



Fast Frontier-based Information-driven Exploration
(2020)

III



FUEL: Fast UAV Exploration
(2021)

Existing Work

I

Receding Horizon Next Best View Planner
(2016)





II

Fast Frontier-based Information-driven Exploration
(2020)

III

FUEL: Fast UAV Exploration
(2021)

Existing Work

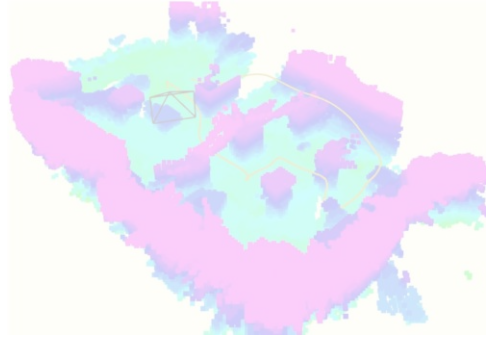
- 
sampling-based
- 
volumetric + travel time
- 
greedy
- 
RRT

II



Fast Frontier-based
Information-driven Exploration
(2020)

III



FUEL: Fast UAV Exploration
(2021)

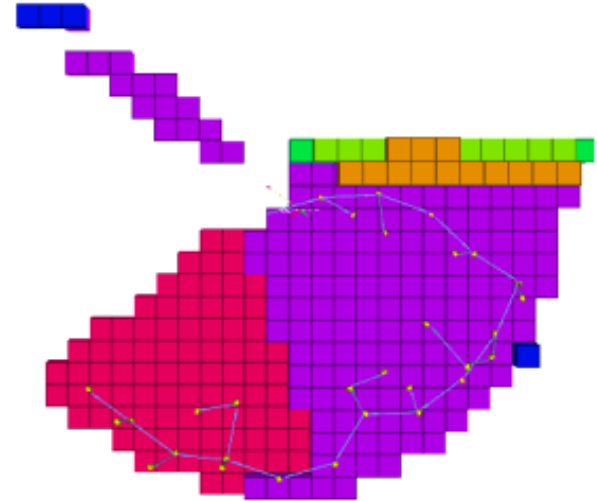
Receding Horizon Next Best View Planner (2016) [1][4]

Description

Receding Horizon Next Best View Planner (2016) [1][4]

Description

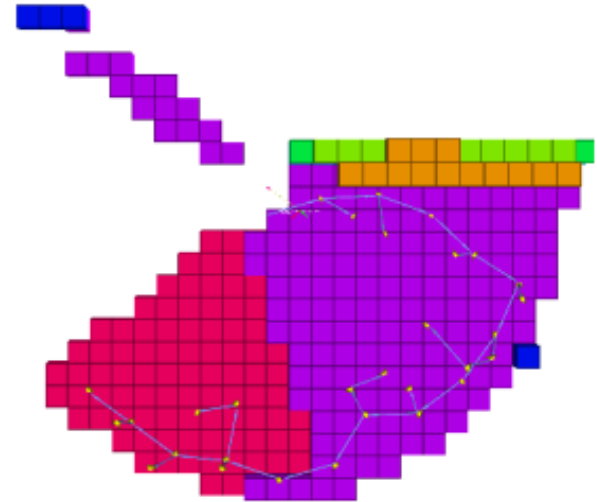
- Sample RRT (x, y, z, yaw) with at N_{min} nodes



Receding Horizon Next Best View Planner (2016) [1][4]

Description

- Sample RRT (x, y, z, yaw) with at N_{min} nodes
- Associate each node n with an information gain $g(n)$ based on number of **visible unexplored voxels** and **path costs**

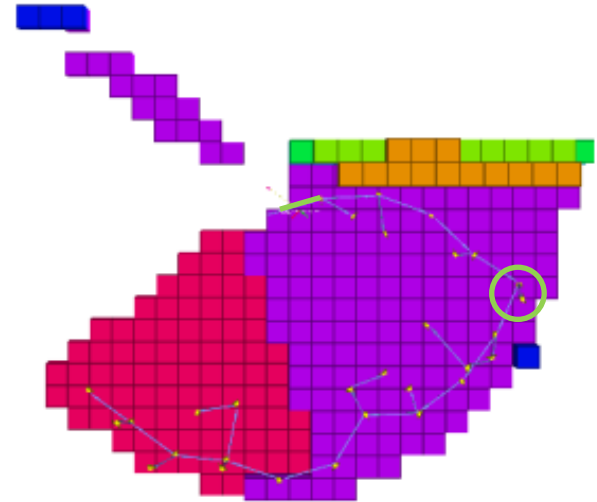


$$\mathbf{Gain}(n_k) = \mathbf{Gain}(n_{k-1}) + \mu(\mathbf{Visible}_V(\mathcal{M}, \xi_k))e^{-\lambda c(\sigma_{k-1}^k)}$$

Receding Horizon Next Best View Planner (2016) [1][4]

Description

- Sample RRT (x, y, z, yaw) with at N_{min} nodes
- Associate each node n with an information gain $g(n)$ based on number of **visible unexplored voxels** and **path costs**
- Select node with highest $g(n)$ and execute first path segment

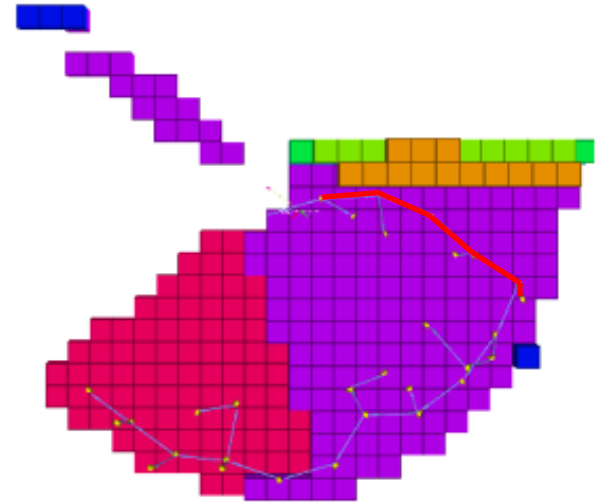


$$\mathbf{Gain}(n_k) = \mathbf{Gain}(n_{k-1}) + \mu(\mathbf{Visible}_V(\mathcal{M}, \xi_k))e^{-\lambda c(\sigma_{k-1}^k)}$$

Receding Horizon Next Best View Planner (2016) [1][4]

Description

- Sample RRT (x, y, z, yaw) with at N_{min} nodes
- Associate each node n with an information gain $g(n)$ based on number of **visible unexplored voxels** and **path costs**
- Select node with highest $g(n)$ and execute first path segment
- Use remaining path as RRT initialization for next planning iteration

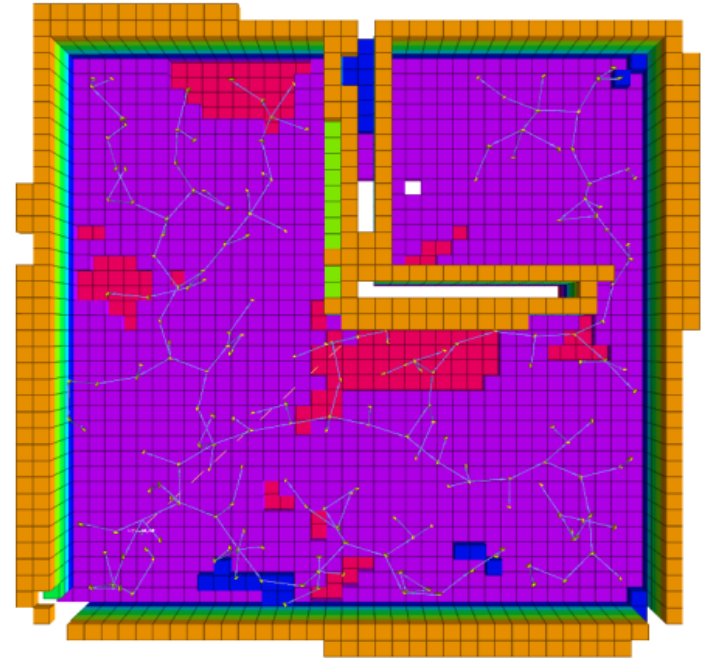


$$\mathbf{Gain}(n_k) = \mathbf{Gain}(n_{k-1}) + \mu(\mathbf{Visible}_V(\mathcal{M}, \xi_k))e^{-\lambda c(\sigma_{k-1}^k)}$$

Receding Horizon Next Best View Planner (2016) [1][4]

Description

- Sample RRT (x, y, z, yaw) with at N_{min} nodes
- Associate each node n with an information gain $g(n)$ based on number of **visible unexplored voxels** and **path costs**
- Select node with highest $g(n)$ and execute first path segment
- Use remaining path as RRT initialization for next planning iteration
- Repeat until RRT reaches N_{max} nodes with $g(n) = 0, \forall n$

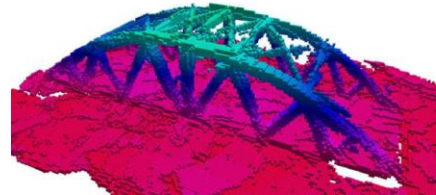
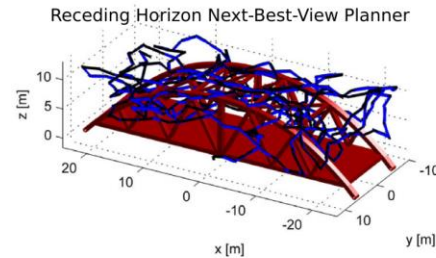


Receding Horizon Next Best View Planner (2016) [1][4]

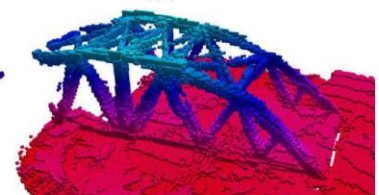
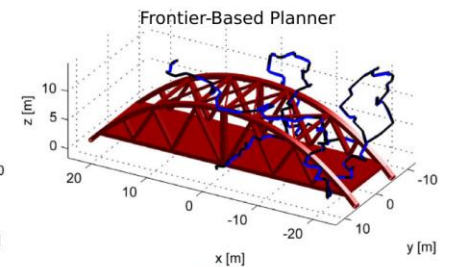
Results

- + Faster computation leads to quicker exploration
- + Huge improvements in scalability
- Prone to back-and-forth movements

$$\mathcal{O}(N_{\text{T}} \log(N_{\text{T}}) + N_{\text{T}}/r^3 \log(V/r^3) + N_{\text{T}}(d_{\text{max}}^{\text{planner}}/r)^4 \log(V/r^3))$$



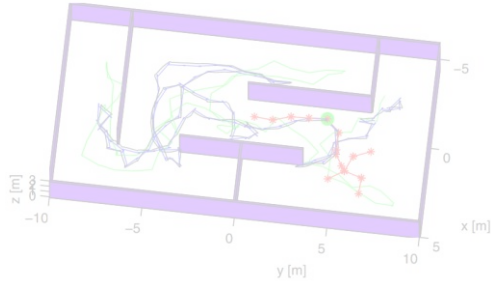
terminated after 43.8 min



terminated after 1670.1 min


Existing Work

I



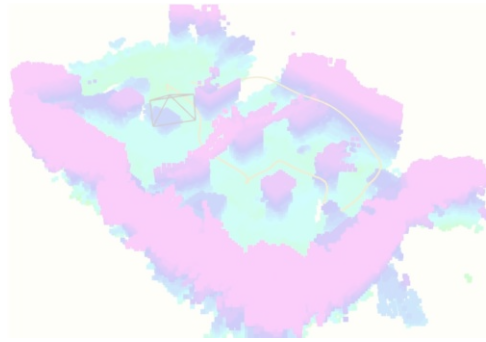
Receding Horizon Next Best View Planner
(2016)

II



Fast Frontier-based Information-driven Exploration
(2020)

III







FUEL: Fast UAV Exploration
(2021)

Existing Work

I

Receding Horizon Next Best View Planner
(2016)

-  hybrid
-  entropy-based + travel time
-  greedy
-  informed RRT*

III

FUEL: Fast UAV Exploration
(2021)

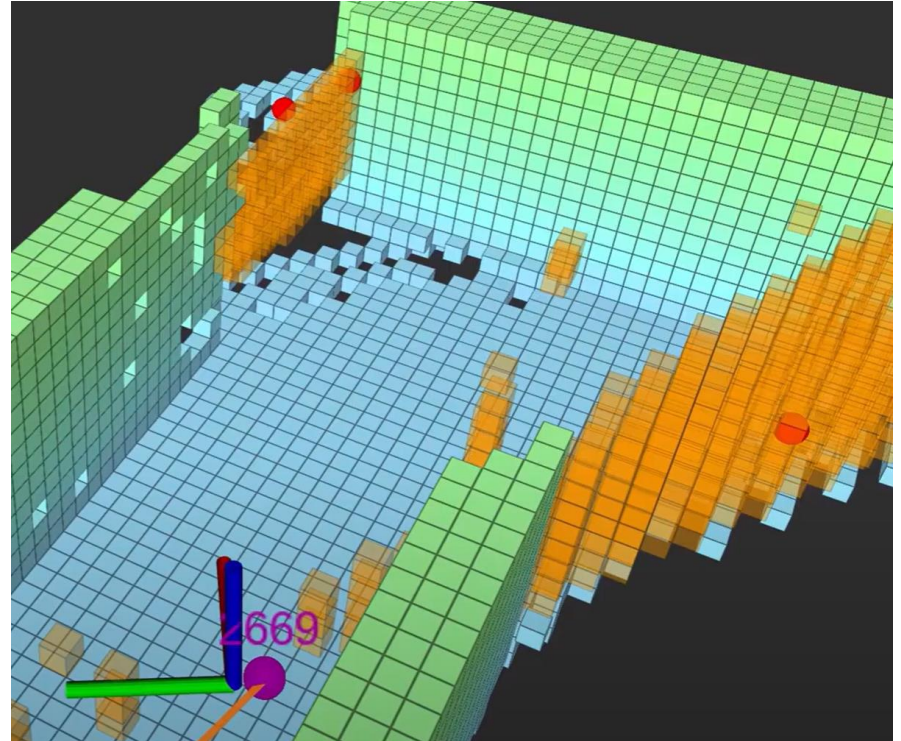
Fast Frontier-based Information-driven Exploration (2020) [2][5]

Description

Fast Frontier-based Information-driven Exploration (2020) [2][5]

Description

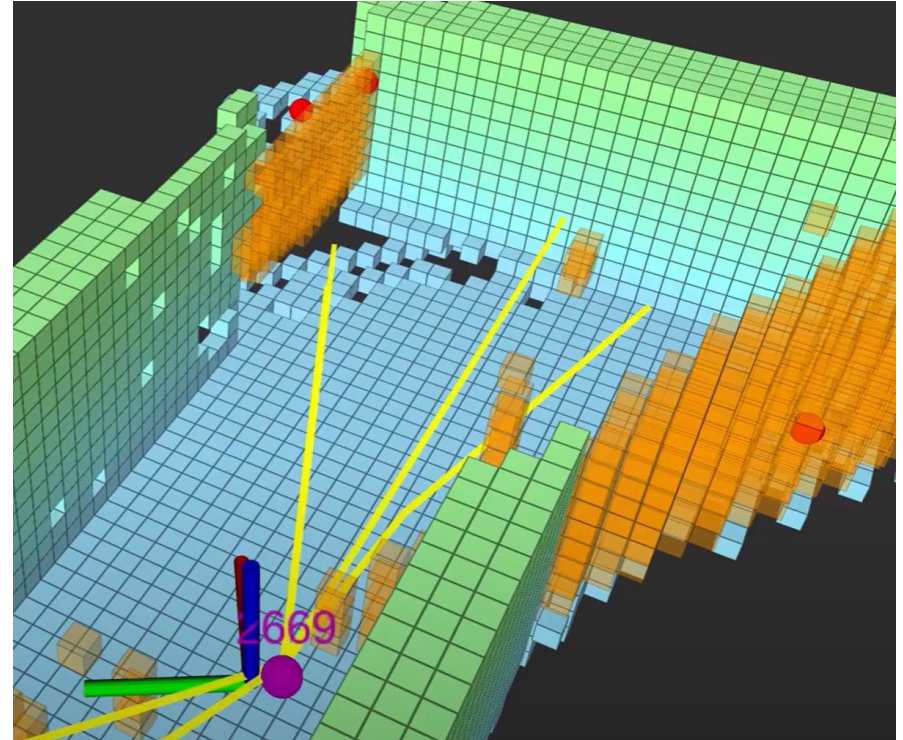
- Leverage **octree map structure** to detect frontier clusters and sample candidates (x, y, z) from frontier clusters



Fast Frontier-based Information-driven Exploration (2020) [2][5]

Description

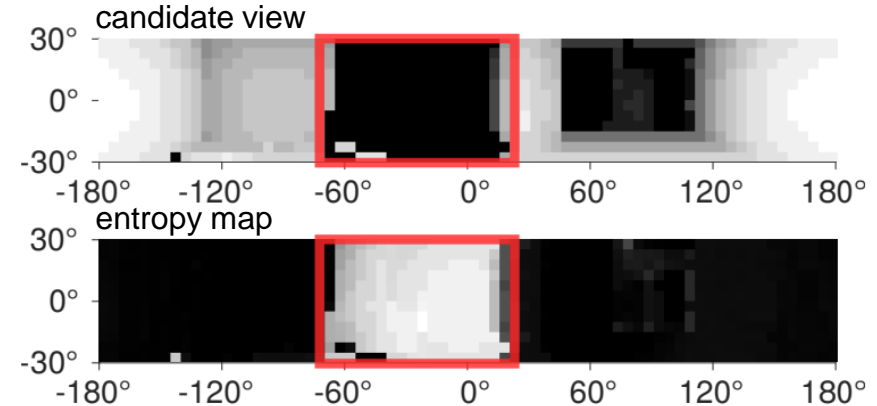
- Leverage **octree map structure** to detect frontier clusters and sample candidates (x, y, z) from frontier clusters
- Employ informed RRT* to find paths to each candidate



Fast Frontier-based Information-driven Exploration (2020) [2][5]

Description

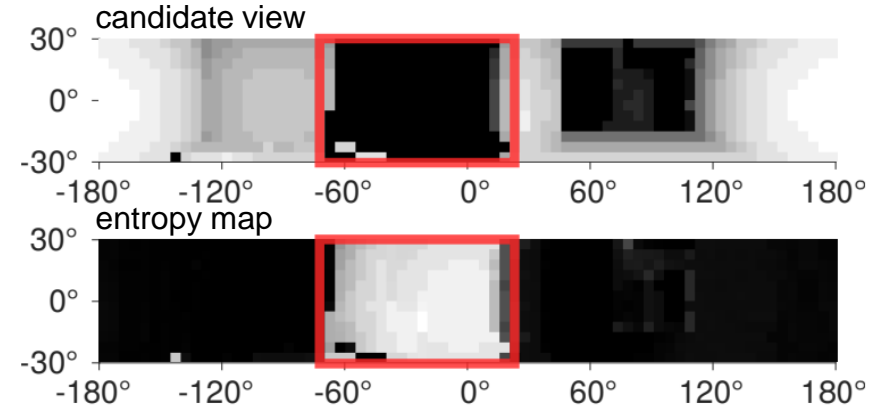
- Leverage **octree map structure** to detect frontier clusters and sample candidates (x, y, z) from frontier clusters
- Employ informed RRT* to find paths to each candidate
- Estimate entropy map around each candidate to and perform **yaw angle optimization** for maximum information gain



Fast Frontier-based Information-driven Exploration (2020) [2][5]

Description

- Leverage **octree map structure** to detect frontier clusters and sample candidates (x, y, z) from frontier clusters
- Employ informed RRT* to find paths to each candidate
- Estimate entropy map around each candidate to and perform **yaw angle optimization** for maximum information gain
- Compute utility values for each candidate based on **entropy** and **path cost** and select best candidate as exploration goal

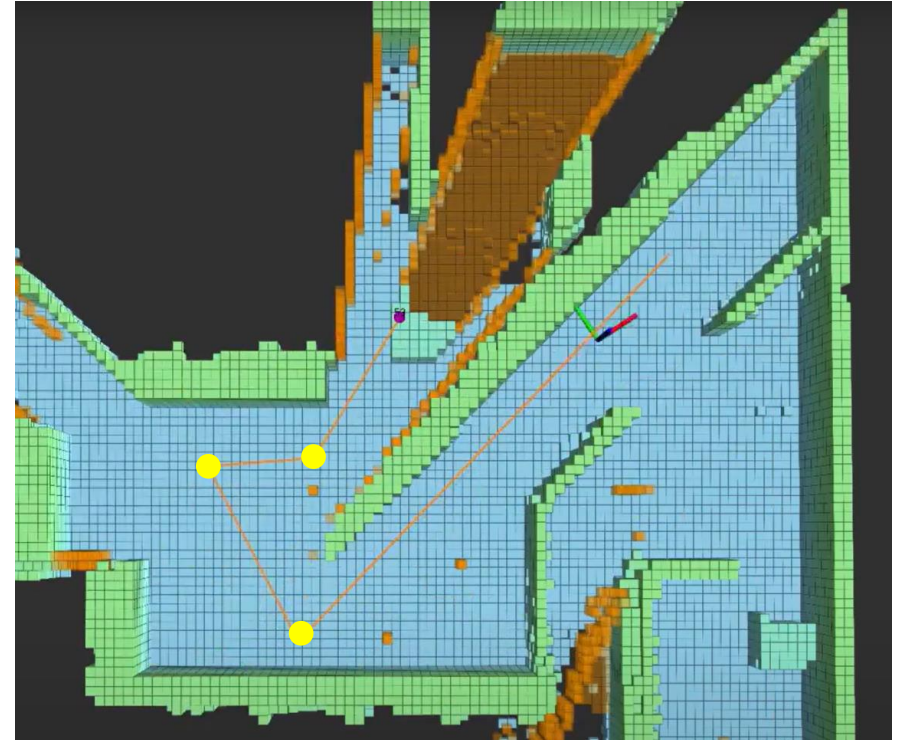


$$u(\mathbf{x}_i, \hat{W}_i) = \frac{\mathbb{H}(\mathbf{x}_i)}{T(\hat{W}_i)}$$

Fast Frontier-based Information-driven Exploration (2020) [2][5]

Description

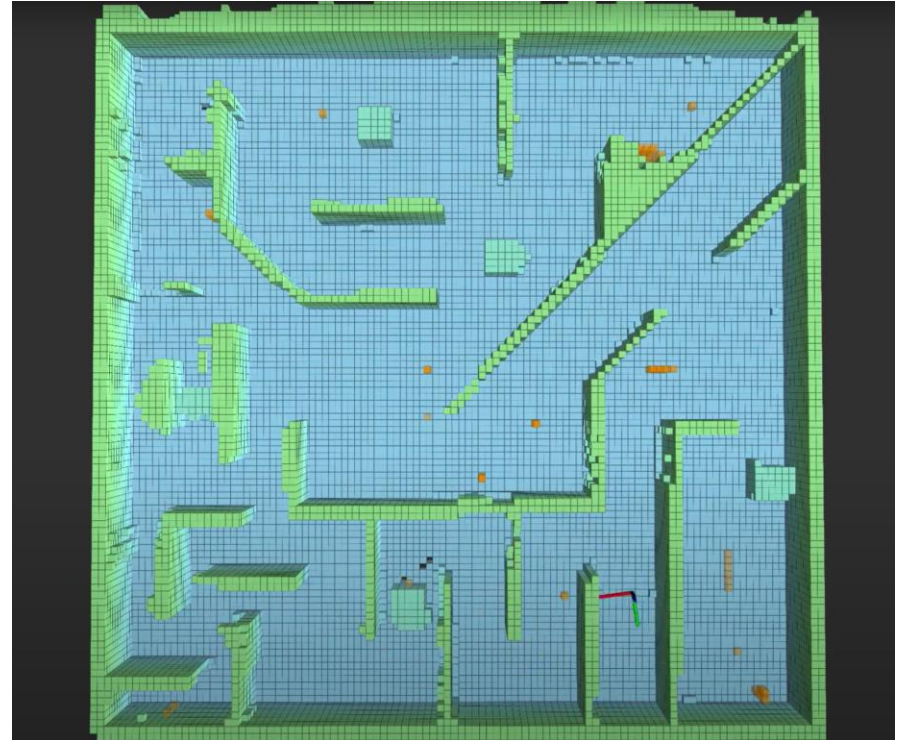
- Leverage **octree map structure** to detect frontier clusters and sample candidates (x, y, z) from frontier clusters
- Employ informed RRT* to find paths to each candidate
- Estimate entropy map around each candidate to and perform **yaw angle optimization** for maximum information gain
- Compute utility values for each candidate based on **entropy** and **path cost** and select best candidate as exploration goal
- Perform **yaw angle optimization** for intermediate waypoints and execute path



Fast Frontier-based Information-driven Exploration (2020) [2][5]

Description

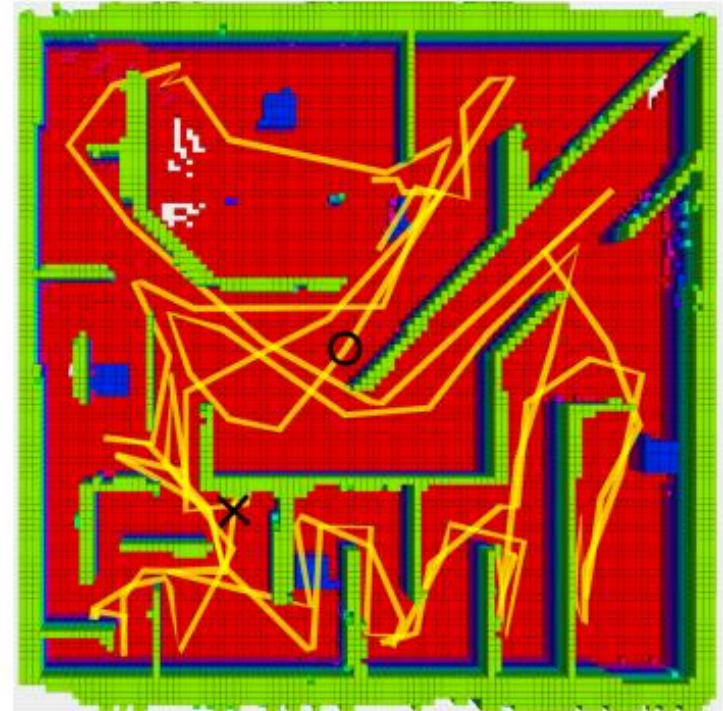
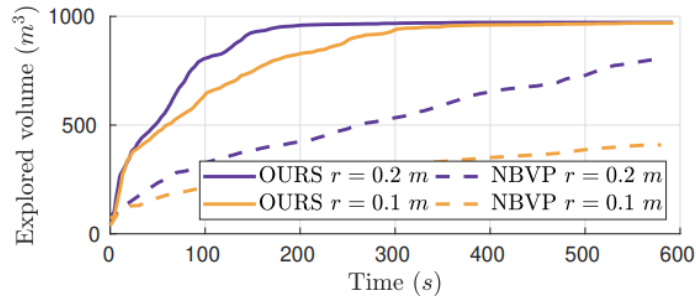
- Leverage **octree map structure** to detect frontier clusters and sample candidates (x, y, z) from frontier clusters
- Employ informed RRT* to find paths to each candidate
- Estimate entropy map around each candidate to and perform **yaw angle optimization** for maximum information gain
- Compute utility values for each candidate based on **entropy** and **path cost** and select best candidate as exploration goal
- Perform **yaw angle optimization** for intermediate waypoints and execute path
- Terminate when all frontier clusters are explored



Fast Frontier-based Information-driven Exploration (2020) [2][5]

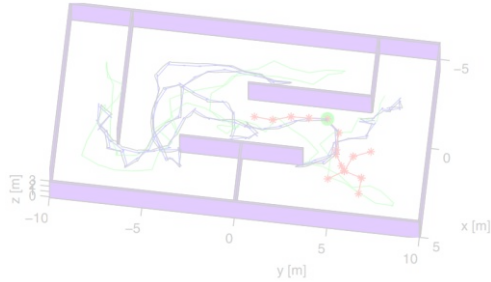
Results

- + Faster and more robust exploration than RH-NBVP due to:
 - guided path planning
 - no expensive frontier clustering
- + Entropy based information gain helps to increase map quality
- No real-time path adaption possible



Existing Work

I



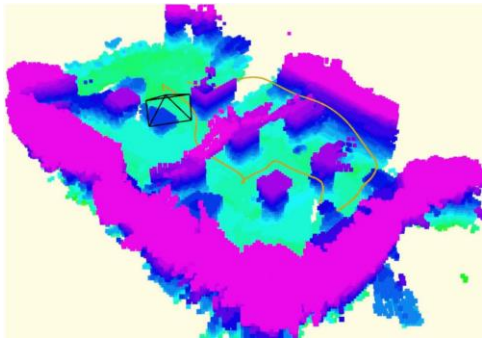
Receding Horizon Next Best
View Planner
(2016)

II



Fast Frontier-based
Information-driven Exploration
(2020)

III



FUEL: Fast UAV Exploration
(2021)





Existing Work

I

Receding Horizon Next Best View Planner
(2016)

II

Fast Frontier-based Information-driven Exploration
(2020)

-  Frontier-based
-  volumetric + travel time + vehicle dynamics
-  global
-  A*

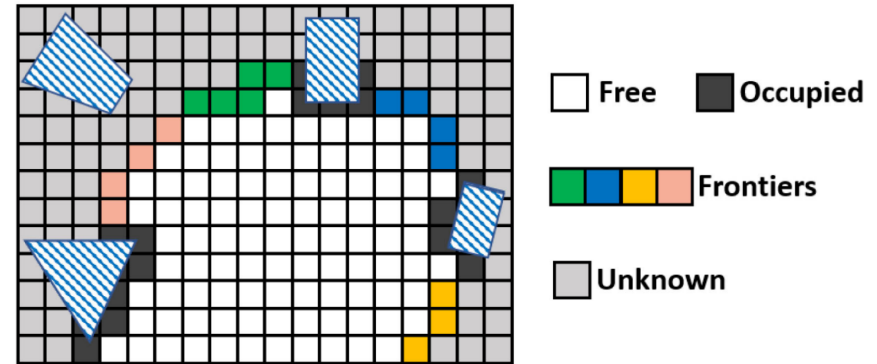
FUEL: Fast UAV Exploration (2021) [3][6]

Description

FUEL: Fast UAV Exploration (2021) [3][6]

Description

- Initial detection of frontier clusters and store them as **FIS**

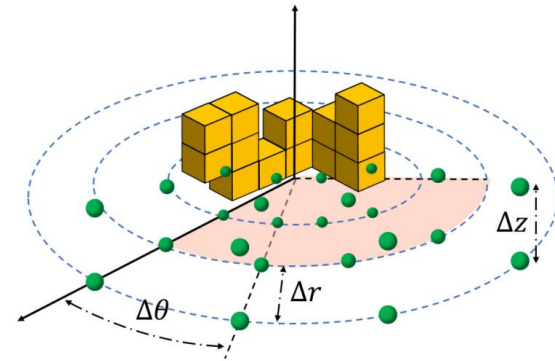


Data	Explanation
C_i	Frontier cells that belong to the cluster
$\mathbf{p}_{\text{avg},i}$	Average position of C_i
B_i	Axis-aligned bounding box of C_i
VP_i	Viewpoints covering the cluster
$L_{\text{cost},i}$	Doubly linked list of connection costs to all other clusters

FUEL: Fast UAV Exploration (2021) [3][6]

Description

- Initial detection of frontier clusters and store them as **FIS**
- Uniformly sample views around cluster center. **Store views with high cluster coverage** in FIS

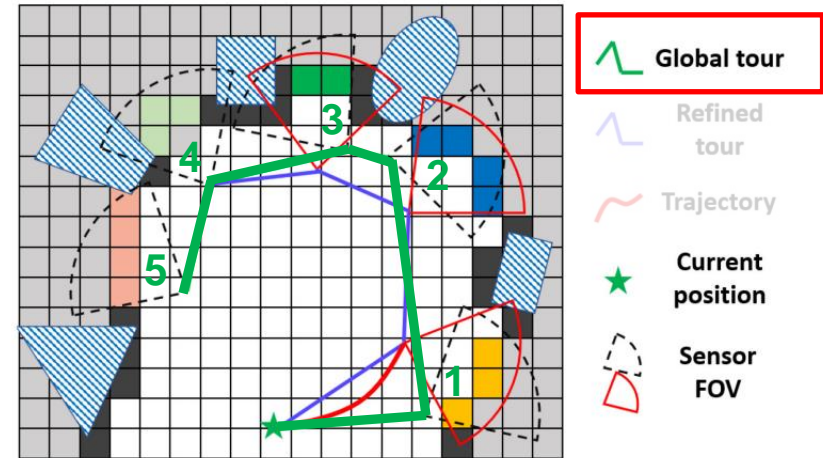


Data	Explanation
C_i	Frontier cells that belong to the cluster
$\mathbf{p}_{\text{avg},i}$	Average position of C_i
B_i	Axis-aligned bounding box of C_i
VP_i	Viewpoints covering the cluster
$L_{\text{cost},i}$	Doubly linked list of connection costs to all other clusters

FUEL: Fast UAV Exploration (2021) [3][6]

Description

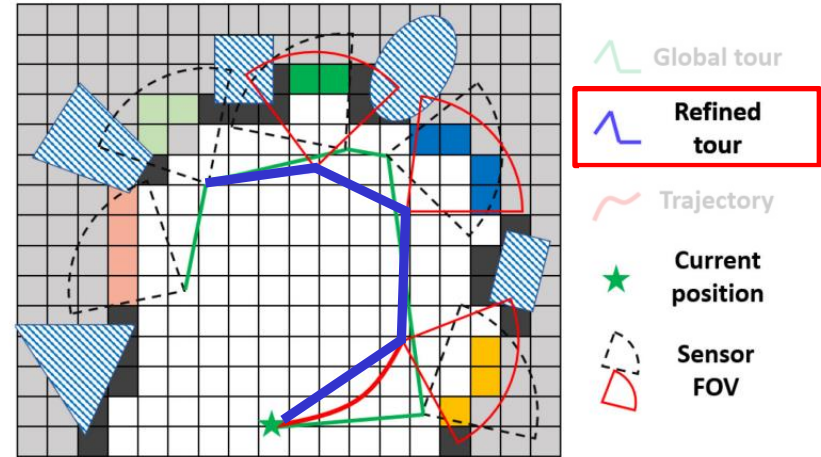
- Initial detection of frontier clusters and store them as **FIS**
- Uniformly sample views around cluster center. **Store views with high cluster coverage** in FIS
- **Global optimization:** Solve TSMP to find optimal exploration order of frontiers



FUEL: Fast UAV Exploration (2021) [3][6]

Description

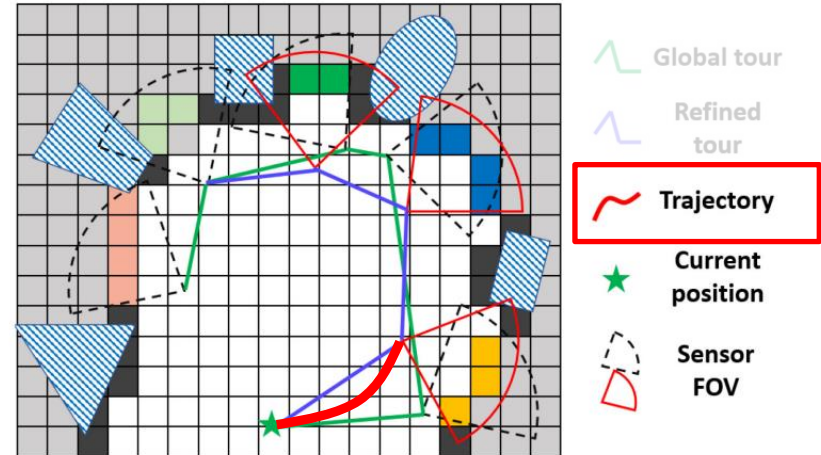
- Initial detection of frontier clusters and store them as **FIS**
- Uniformly sample views around cluster center. **Store views with high cluster coverage** in FIS
- **Global optimization:** Solve TSMP to find optimal exploration order of frontiers
- **Refine local path segment:** Build directed acyclic graph of richer viewpoint sets and find cheapest path (Dijkstra)



FUEL: Fast UAV Exploration (2021) [3][6]

Description

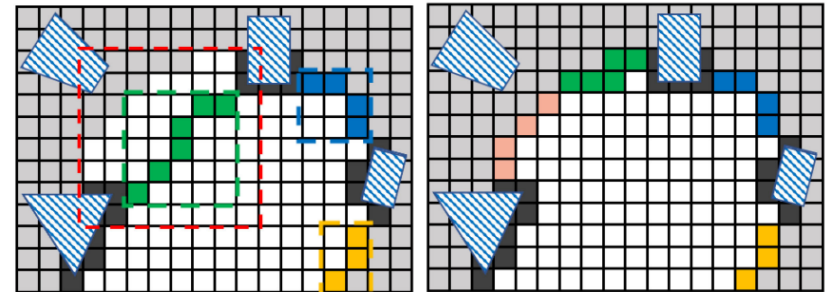
- Initial detection of frontier clusters and store them as **FIS**
- Uniformly sample views around cluster center. **Store views with high cluster coverage** in FIS
- **Global optimization:** Solve TSMP to find optimal exploration order of frontiers
- **Refine local path segment:** Build directed acyclic graph of richer viewpoint sets and find cheapest path (Dijkstra)
- **B-Spline Trajectory:** Compute Splines between next waypoints to allow for smoother and faster flying



FUEL: Fast UAV Exploration (2021) [3][6]

Description

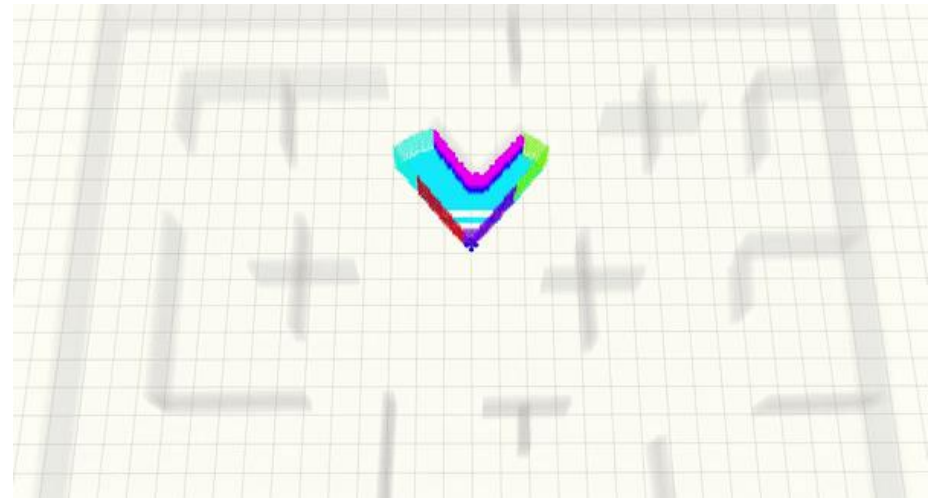
- Initial detection of frontier clusters and store them as **FIS**
- Uniformly sample views around cluster center. **Store views with high cluster coverage** in FIS
- **Global optimization:** Solve TSMP to find optimal exploration order of frontiers
- **Refine local path segment:** Build directed acyclic graph of richer viewpoint sets and find cheapest path (Dijkstra)
- **B-Spline Trajectory:** Compute Splines between next waypoints to allow for smoother and faster flying
- At each map update, **incrementally** update all FISs in that area and repeat planning process



FUEL: Fast UAV Exploration (2021) [3][6]

Description

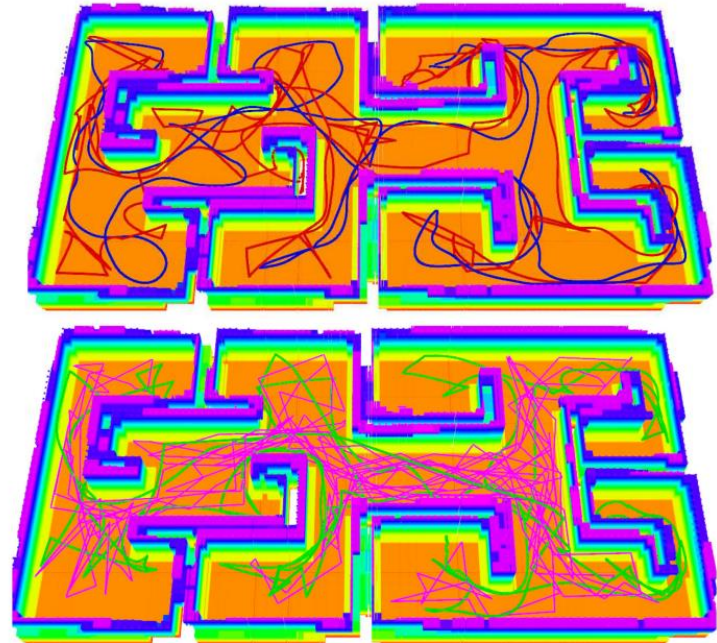
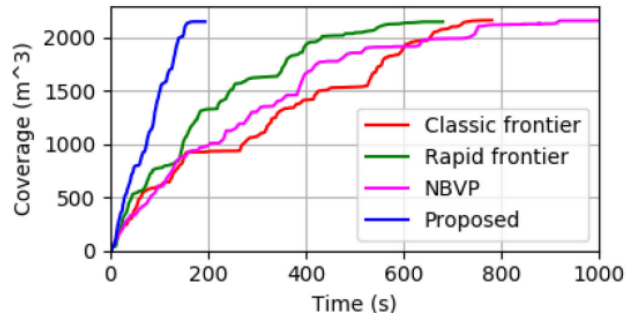
- Initial detection of frontier clusters and store them as **FIS**
- Uniformly sample views around cluster center. **Store views with high cluster coverage** in FIS
- **Global optimization:** Solve TSMP to find optimal exploration order of frontiers
- **Refine local path segment:** Build directed acyclic graph of richer viewpoint sets and find cheapest path (Dijkstra)
- **B-Spline Trajectory:** Compute Splines between next waypoints to allow for smoother and faster flying
- At each map update, **incrementally** update all FISs in that area and repeat planning process
- Terminate when no frontiers are left



FUEL: Fast UAV Exploration (2021) [3][6]

Results

- + Hierarchical Planning:
 - smoother exploration path
 - continuous path updates (adaptive)
- + Global Optimization:
 - shorter exploration path
- + Incremental Frontier Structure:
 - reduced computational overhead



Conclusions

- Frontier detection is important to guide the exploration process to unexplored space
- Sampling based methods can increase computational efficiency
- Hybrid approaches are getting more and more popular
- Global optimization leads to better path efficiency
- More elaborate information gain can be used to tune exploration
(e.g. taking vehicle dynamics into account speeds up exploration significantly)

Further Work

- Multi Resolution Mapping [7]
- Exploit larger scale experiments [8]
- More elaborate information gains (e.g. include object semantics) [10]
- Distributed multi agent exploration [13]
- Incorporate Deep Learning Approaches
 - Leverage Scene Completion Networks for more informed exploration [11]
 - Reinforcement Learning approaches [12]

Questions ?

References

- [1] A. Bircher, M. Kamel, K. Alexis, H. Oleynikova, and R. Siegwart, "Receding horizon path planning for 3D exploration and surface inspection," *Autonomous Robots*, vol. 42, no. 2, pp. 291–306, Feb. 2018.
- [2] A. Dai, S. Papatheodorou, N. Funk, D. Tzoumanikas, S. Leutenegger, „Fast frontier-based information-driven autonomous exploration with an MAV” , 2020 IEEE International Conference on Robotics and Automation (ICRA), pp. 9570–9576, Feb. 2020.
- [3] B. Zhou, Y. Zhang, X. Chen, and S. Shen, "FUEL: Fast UAV exploration using incremental frontier structure and hierarchical planning," *IEEE Robot. Autom. Lett.*, vol. 6, no. 2, pp. 779–786, Apr. 2021.
- [4] <https://github.com/HKUST-Aerial-Robotics/FUEL>
- [5] <https://github.com/ethz-asl/nbvplanner>
- [6] <https://www.youtube.com/watch?v=tH2VkvOny38>
- [7] E. Vespa, N. Funk, P. H. Kelly, and S. Leutenegger, "Adaptive-resolution octree-based volumetric SLAM," in 2019 International Conference on 3D Vision (3DV). IEEE, Sep 2019, pp. 654–662
- [8] J. Huang *et al.*, "FAEL: Fast Autonomous Exploration for Large-scale Environments With a Mobile Robot," in *IEEE Robotics and Automation Letters*, vol. 8, no. 3, pp. 1667-1674, March 2023.
- [9] X. Yu, C. Chen, „Semantic-aware Next-Best-View for Multi-DoFs Mobile System in Search-and-Acquisition based Visual Perception”, 2024.
- [10] L. Schmid, M. N. Cheema, V. Reijgwart, R. Siegwart, F. Tombari, and C. Cadena, "SC-explorer: Incremental 3D scene completion for safe and efficient exploration mapping and planning," 2022
- [11] Y. Cao, R. Zhao, Y. Wang, B. Xiang, and G. Sartoretti, "Deep reinforcement learning-based large-scale robot exploration," *IEEE Robotics and Automation Letters*, 2024
- [12] B. Zhou, H. Xu, and S. Shen, "Racer: Rapid collaborative exploration with a decentralized multi-uav system," *IEEE Transactions on Robotics*, 2023
- [13] <https://www.eenewseurope.com/en/drones-with-ears-to-aid-in-natural-disasters/>
- [14] <https://de.wikipedia.org/wiki/Mars-Rover>